# Riding the Monsoon

Geography and Iron Age Trade in the Indian Ocean

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# Introduction



Introduction

#### Motivation

#### **Research Question:**

How did the unique geography of the Indian Ocean influence trade and development in the late Iron Age?

- Trade in the ancient world was hindered by high trade costs and technological limitations
  - This reduced the attractiveness and profitability of long-distance, trans-oceanic trade
- ➤ The unique geography and climatic conditions of the Indian Ocean made this region an exception to this
  - Orientation of land masses around the Indian Ocean
  - Regularity of monsoon winds
- Climate and geography can overcome technological barriers and reduce trade costs to help sustain complex trade networks







- Construct a new dataset of ancient Indian Ocean trade from textual sources
- Calculate wind-dependent transportation costs and routes
- Develop a modified Ricardian gravity model to estimate trade
- Estimate the relationship between ancient trade flows and development



### Key Results

Introduction 00000

- Wind speed-dependent distance costs matter: monsoon winds facilitated sophisticated long-distance trade.
- ► The relationship between distance and trade volume is non-linear: this is linked to both a proximity effect and an endowment effect
- Diversity of exports is linked to higher levels of development: heavy reliance on imports seems to be connected to lower levels of development.
- Evidence for an ancient resource curse: cities that are more dependent on cash crops are under-developed.



# Related Literature

Introduction

This paper is the first to use ancient textual sources to model trade in the Indian Ocean and provide insight into potential trade-driven determinants of growth in the region at the time.

- Pre-modern Trade
  - Barjamovic et al. (2019)
  - Bakker et al. (2018)
  - Pascali (2017)
- Ancient Trade Data
  - ► Fluckiger et al. (2019)
  - Broodbank (2006)
  - ► Temin (2006; 2013)

- Trade Costs
  - Maurer and Rauch (2019)
  - Juhasz (2018)
  - Liu and Meissner (2015)
- Trade and Development
  - Redding and Venables (2004)
  - Wacziarg and Welch (2008)
  - Feyrer (2019)



#### **Outline**

Introduction 00000

- 1) Data and Ancient Trade
- 2) Gravity Estimation
- 3) Trade Network Results
- 4) Trade and Development
- 5) Conclusion



#### **Data and Ancient Trade**

#### Trade Data

- Data from the Periplus of the Erythraean Sea (mid-first century)
- 150 individual products; 37 product types
- 47 identified cities: three levels of record
  - goods listed with partner city
  - goods listed with partner region
  - goods listed without any partner
- Data Issues:
  - Quality indicators
  - Quantity indicators
  - Omitted data









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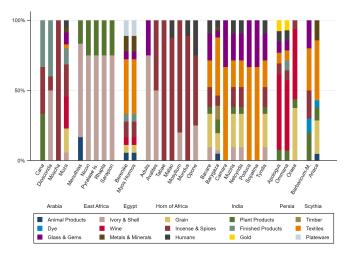
8. After Avalites there is another market-town, better than this, called Malao, distant a sail of about eight hundred stadia. The anchorage is an open roadstead, sheltered by a spit running out from the east. Here the natives are more peaceable. There are imported into this place the things already mentioned, and many tunics, cloaks from Arsinoe, dressed and dyed; drinking-cups, sheets of soft copper in small quantity, iron, and gold and silver coin, not much. There are exported from these places myrrh, a little frankincense, (that known as far-side), the harder cinnamon, duaca, Indian copal and macir, which are imported into Arabia; and slaves, but rarely.

36. Sailing through the mouth of the Gulf, after a six-days' course there is another market-town of Persia called Ommana. To both of these market-towns large vessels are regularly sent from Barygaza, loaded with copper and sandalwood and timbers of teakwood and logs of blackwood and ebony. To Ommana frankincense is also brought from Cana, and from Ommana to Arabia boats sewed together after the fashion of the place; these are known as madarata. From each of these market-towns, there are exported to Barygaza and also to Arabia, many pearls, but inferior to those of India: purple, clothing after the fashion of the place, wine, a great quantity of dates, gold and slaves.

Text from PME (Schoff, 1912)



# **Export Shares by City**





#### Trade Variables

Bilateral Trade Flows:

$$X_{ij} = \sum_{g} x_{ijg}$$

with  $x_{ijg} = \begin{cases} 1 & \text{if good } g \text{ is traded between cities } i \text{ and } j; \\ 0 & \text{otherwise.} \end{cases}$ 

Trade Basket Diversity:

$$h_i = 1 - \sum_n \left(\frac{\lambda_{in}}{L_i}\right)^2$$

where  $\lambda_{in}$  is the number of products in category n and  $L_i$  is the total number of products.



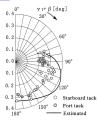
# **Transportation Cost Data**

- Seasonal Monsoon Wind Data
  - CERSAT/Laboratoire D'Océanographie Spatiale
    - ERS-1/ERS-2/NSCAT satellite data
  - 1992-1995
    - June to July: Summer (SW) Monsoon
    - January to February: Winter (NE) Monsoon

► Summer Monsoon

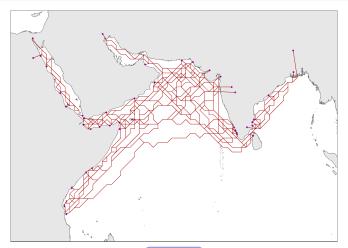
► Winter Monsoo

- Calculating Sailing Speed
  - Nomoto, Masuyama, and Sakurai (2000)
    - Naniwa-maru sea trials in 1999
    - Square-rigged cargo ship from Edo period





# Sea Routes (Summer Monsoon)



▶ Winter Routes



# Sailing Times

Origin	Destination	Travel Time	
		Attested	Calculated
Berenike Myos Hormos Myos Hormos Tabae	Malao Muza Barygaza Rhapta	1 Month 1 Month >2 Months <1 Month	36.03 Days 30.84 Days 64.70 Days 17.99 Days

Note: Travel times are calculated according to monsoon wind data in the ideal sailing season for the direction of travel. Attested travel times come from Cobb (2018).

Transportation costs are calculated as the length of time needed for a return trip between two cities in the correct season



# **Historical Development**

- ► 0.5 degree by 0.5 degree grid
- Sample:
  - 500 km radius around cities

► Hinterland Variations

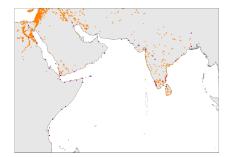


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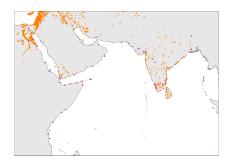
► Hinterland Variations







# Historical Development



- ▶ 37000 ancient sites
  - pre-Bronze Age to Late Medieval
- Four broad categories:
  - Settlements; Buildings; Geography; Polities
  - 24400 settlements and buildings
- 6600 sites of the right type within the right location and date range



### Historical Development

#### Growth Variable:

- Difference in the number of sites in a grid cell before and after the cut-off date
- Cut-off date: 30 BCE
- Maximum date: 640 CE

$$y_c = \sigma_c^{post} - \sigma_c^{pre}$$



#### Site Distribution

Region	Sites	Standard Deviation
Egypt Horn of Africa	290.200 1.571	378.342 1.988
East Africa	0.200	0.447
Arabia	8.500	11.149
Persia	94.333	151.296
Scythia	7.500	3.536
India	13.667	9.076
All Regions	46.907	152.495

Note: Sites is the average number of sites within 500 km of cities in the given region.

- Summing of different site types: lack of non-Mediterranean data
- Selection bias: Roman infrastructure & archaeological focus



### **Gravity Estimation**

#### **Gravity Model**

- Ricardian gravity model
- ► Model
- Eaton and Kortum (2002)
- Anderson and van Wincoop (2003)
- Barjamovic et al (2019)
- Cities choose import baskets based on price distributions
  - Technology, input prices (labour), transportation distance
- More competitive cities will trade more varieties (not just more goods)
  - City size (labour)
  - Transport costs (distance)



# **Gravity Model**

#### **Gravity estimation equation:**

$$E[X_{ij}] = exp\{\beta_0 + \beta_1 ln(d_{ij}) + \mu_i + \mu_j + \epsilon_{ij}\}$$

- Unique features of the Indian Ocean reduce trade costs
  - Seasonal regularity of the monsoon
  - Orientation of landmasses around the Indian Ocean



# **Gravity Results**

	(1)	(2)	(3)
In(SailDist)	-0.273**	0.334	-8.534**
	(0.114)	(0.241)	(3.156)
sqrt(In(SailDist))			30.029** (10.563)
City FE	Yes	Yes	Yes
N	107	556	556
R <sup>2</sup>	0.856	0.225	0.257

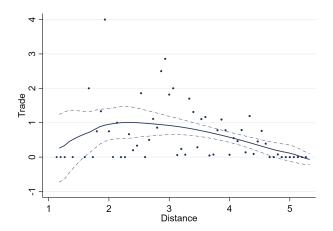
Standard errors in parentheses

Note: Dependent variable is the total number of good varieties traded; In(SailDist) is the log of the total round-trip sailing time for the fastest calculated route accounting for wind speed.



<sup>\*</sup> Significant at 0.10; \*\* Significant at 0.05

#### Non-linear Distance





#### Non-linear Distance

Proximity Variable:

$$Neighbour_{ij} = \begin{cases} 1 & \text{if } d_{ij} \leq 14 \text{ days;} \\ 0 & \text{otherwise.} \end{cases}$$

**Endowment Index:** 

$$EI_{ij} = 1 - \sum_{n} \frac{|\lambda_{in} - \lambda_{jn}|}{L_i + L_j}$$

Where  $\lambda_{in}$  is the number of products within the product category n exported by city i and  $L_i$  is the total number of products exported by city i



	(1)	(2)	
In(SailDist)	-1.151** (0.465)	-1.098** (0.473)	
Neighbour	-2.858** (0.734)	-1.912** (0.797)	
Endowment Inde	ex	-10.316** (1.562)	
City FE	Yes	Yes	
N	556	556	
$R^2$	0.293	0.430	

Standard errors in parentheses

Note: Dependent variable is the total number of good varieties traded; In(SailDist) is the log of the total round-trip sailing time for the fastest calculated route accounting for wind speed; Neighbour is a dummy variable for cities in close proximity; Endowment Index is an index of similarity of endowments.



<sup>\*</sup> Significant at 0.10; \*\* Significant at 0.05

#### **Trade and Development**

# **Export-led Growth**

Distance to Periplus ports:

$$y_c = \beta_1 \ln(d_c) + \nu_c + \epsilon_c$$

Export and Import basket diversity:

$$y_c = \beta_1 \omega_c h_c^x + \beta_2 \omega_c h_c^m + \nu_c + \epsilon_c$$

 $\omega_c$  is a distance weight term given by  $\frac{1}{d_c}$  (where  $d_c$  is the distance to the nearest port in the Periplus.



#### Ancient Resource Curse

Sectoral shares:

$$S(r)_i = \frac{\lambda_{ir}}{L_i}$$

The share  $S(r)_i$  of sector r for city i is the number of products  $\lambda_{ir}$  in sector r exported or imported by city i divided by the total number of products exported by city i,  $L_i$ 

Estimation equation:

$$y_c = \beta_1 \omega_c S(mfg)_c^x + \beta_2 \omega_c S(spc)_c^x + \beta_3 \omega_c S(bul)_c^m + \nu_c + \epsilon_c$$



	(1)	(2)	(3)
In(Dist)	-0.094* (0.054)		
Export Diversity		31.273** (11.199)	
Import Diversity		-15.278** (6.691)	
Manufactures			3.115** (1.462)
Spices & Aromatics			-22.187* (13.262)
Bullion			638.741** (315.511)
Rome	0.388** (0.192)	0.467** (0.187)	0.465** (0.187)
Cell FE	Yes	Yes	Yes
N R <sup>2</sup>	3172 0.065	3172 0.069	3172 0.067

Standard errors in parentheses



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Robustness Checks

#### **Robustness Checks**

#### Robustness Checks

Product Shares

$$X_{ij} = rac{\sum_{g} x_{ijg}}{Z_i + Z_j}$$
 with  $x_{ijg} = egin{cases} 1 & ext{if good } g ext{ is traded between cities } i ext{ and } j; \\ 0 & ext{otherwise.} \end{cases}$ 

- Third Century Decline
  - Adjusted maximum cut-off date: 300 CE
- Variations in Hinterland Size
  - Reduce sample grid radius size around cities
  - 350 km and 150 km



#### Robustness: Product Shares

	(1)	(2)
In(SailDist)	-0.260** (0.104)	-1.407** (0.533)
Neighbour		-2.371** (0.799)
Endowment Index		-12.690** (1.897)
City FE N R <sup>2</sup>	Yes 107 0.850	Yes 446 0.980

Standard errors in parentheses

Note: Dependent variable is the share of total good varieties traded; In(SailDist) is the log of the total round-trip sailing time for the fastest calculated route accounting for wind speed; Neighbour is a dummy variable for cities in close proximity; Endowment Index is an index of similarity of endowments.



<sup>\*</sup> Significant at 0.10; \*\* Significant at 0.05

Robustness Checks 0000

### Robustness: Third Century Decline

	(1)	(2)	(3)
In(Dist)	-0.091* (0.054)		
Export Diversity		31.640** (11.193)	
Import Diversity		-15.517** (6.688)	
Manufactures			3.082** (1.461)
Spices & Aromatics			-22.260* (13.255)
Bullion			641.890** (315.347)
Rome	0.381** (0.192)	0.458** (0.187)	0.456** (0.187)
Cell FE	Yes	Yes	Yes
N	3172	3172	3172
R <sup>2</sup>	0.065	0.068	0.067

Standard errors in parentheses

Note: Dependent variable is the standardised change in ancient place records within a grid cell with a date limit of 300 CE imposed: In(Dist) is the distance from the nearest Periplus port: Export and Import Diversity are distance-weighted Herfindahl-style indices of export/import product concentration; Manufactures and Spices & Aromatics are distance-weighted measures of export shares for the given sector; Bullion is the distance-weighted measure of import share of bullion products; Rome is a dummy for the grid cell being a part of the Roman Empire.



<sup>\*</sup> Significant at 0.10: \*\* Significant at 0.05

#### Robustness: Hinterland Variations

	350 km	350 km			150 km		
	(1)	(2)	(3)	(4)	(5)	(6)	
In(Dist)	-0.158** (0.074)			-0.306** (0.144)			
Export Diversity	′	42.234** (12.678)			55.579** (17.047)		
Import Diversity	′	-21.947** (7.574)			-30.188** (10.151)		
Manufactures			3.024* (1.577)			2.876* (1.572)	
Spices & Aroma	atics		-32.943** (15.394)			-45.012** (21.056)	
Bullion			724.274** (367.894)			1108.955** (539.840)	
Cell FE N R <sup>2</sup>	Yes 2042 0.109	Yes 2042 0.114	Yes 2042 0.111	Yes 601 0.397	Yes 601 0.410	Yes 601 0.404	

Standard errors in parentheses

Note: Dependent variable is standardised change in ancient place records within a grid cell: In(Dist) is the distance from the nearest Periplus port: Export and Import Diversity are distance-weighted Herfindahl-style indices of export/import product concentration; Manufactures and Spices & Aromatics are distanceweighted measures of export shares for the given sector; Bullion is the distance-weighted measure of import share of bullion products; Controls for the grid cell being a part of the Roman Empire are included.



<sup>\*</sup> Significant at 0.10; \*\* Significant at 0.05

#### Conclusion

#### Discussion

- Distance has an impact on trade in the Indian Ocean
  - Sailing time was an important factor in trade
  - Distance reduced a city's comparative advantage in markets (in a Ricardian sense)
- Non-linear effects of distance
  - Cities that are too close together appear to trade less
    - Similarities in endowment
    - Missing data: bias in data collection in the Periplus



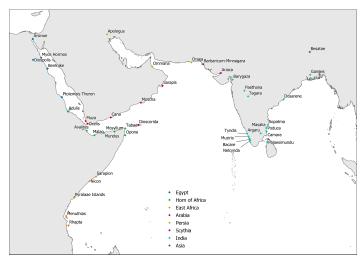
#### Discussion

- Ancient export-oriented growth
  - Diversity of exports matters
  - More variety is linked to higher later development
- Under-development and the resource curse
  - Reliance on ancient 'cash crops' (spice, incense, resin, etc.) is linked to lower development levels
  - Pliny and the 100 million sesterces per year
    - Bullion imports are linked to significantly higher development



### **Thank You**

# Periplus City Map



#### **Product Data Table**

Product	Product Category	Х	M	Product	Product Category	Х	M
Clarified Butter	Animal Products	6	2	Arabian Clothing	Textiles	1	2
Horses	Animal Products	1	2	Blankets	Textiles	1	2
Mountain Tortoise	Ivory & Shell	1	1	Cloaks	Textiles	6	3
Tortoise Shell	Ivory & Shell	12	9	Coloured Sashes	Textiles	1	2
lvory	Ivory & Shell	9	6	Girdles	Textiles	7	2
Elephant Ivory	Ivory & Shell	1	1	Local Clothing	Textiles	2	3
Rhino Ivory	Ivory & Shell	6	2	Robes	Textiles	1	1
Rice	Grain	7	7	Skin Coats	Textiles	1	1
Wheat	Grain	14	9	Thin Clothing	Textiles	1	2
Indian Copal	Plant Products	2	1	Tunics	Textiles	5	1
Aloes	Plant Products	1	12	Indian Cloth	Textiles	1	6
Macir	Plant Products	2	1	Cloth	Textiles	2	5
Palm Oil	Plant Products	5	1	Cotton Cloth	Textiles	7	2
Sesame Oil	Plant Products	7	6	Mallow Cloth	Textiles	2	2
Dates	Plant Products	2	2	Monache Cloth	Textiles	7	2
Sour Grape Juice	Plant Products	6	1	Muslins	Textiles	3	4
Sugarcane Juice	Plant Products	6	2	Purple Cloth	Textiles	1	2
Blackwood	Timber	2	1	Raw Silk	Textiles	1	5
Ebony	Timber	2	1	Sagmatogene Cloth	Textiles	7	2
Sandalwood	Timber	2	1	Silk Cloth	Textiles	4	5
Teakwood	Timber	2	1	Silk Yarn	Textiles	1	5
Coloured Lac	Dye	1	1	Carnelian	Gems & Glass	1	1
Purple	Dve	2	2	Coral	Gems & Glass	1	2
Wine	Wine	8	6	Diamonds	Gems & Glass	3	4
Duaca	Incense & Spices	2	1	Pearls	Gems & Glass	5	6
Fragrant Ointments	Incense & Spices	1	2	Sapphires	Gems & Glass	3	4
Frankincense	Incense & Spices	4	13	Transparent Stones	Gems & Glass	3	4
Myrrh	Incense & Spices	3	3	Flint Glass	Gems & Glass	1	1
Spikenard	Incense & Spices	3	4	Glass	Gems & Glass	5	1
Storax	Incense & Spices	1	2	Murrhine Glass	Gems & Glass	1	1
Cinnamon	Incense & Spices	2	3	Copper	Metals & Minerals	3	3
Malabathrum	Incense & Spices	4	8	Iron	Metals & Minerals	1	i
Pepper	Incense & Spices	3	4	Steel	Metals & Minerals	1	1
Spices	Incense & Spices	1	2	Tin	Metals & Minerals	1	2
Awis	Finished Products	5	ī	Enslaved Persons	Humans	6	11
Daggers	Finished Products	5	1	Coin/Gold	Bullion	2	2
Hatchets	Finished Products	5	1	Gold Plate	Plateware	1	2
Images	Finished Products	1	2	Silver Plate	Plateware	i	2
I ances	Finished Products	5	1	MIC			-
Sewn Boats	Finished Products	1	- 1				
Native Produce	Finished Products	1	12				

Note: This table includes all individual products listed in the text of [?] with origins and destinations identified. X indicates the number of cities exporting the product; M indicates the number of cities exporting the product; M indicates



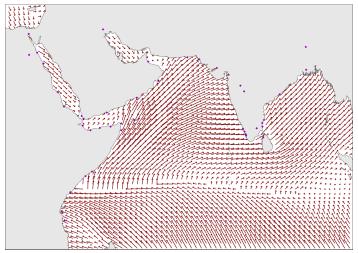
# City Data Table

City	Region	Coordinates	Goods	Partners
Arsinge	Egypt	29.97. 32.55	3	7
Berenike	Egypt	23.91, 35.48	22	3
Diospolis	Egypt	25.72, 32.61	3	7
Myos Hormos	Egypt	26.16, 34.24	22	3
Adulis	Horn of Africa	15.26, 39.66	32	3
Avalites	Horn of Africa	11.35, 43.47	22	6
Malao	Horn of Africa	10.44, 45.02	30	9
Mosyllum	Horn of Africa	11.17, 49.11	34	5
Mundus	Horn of Africa	10.9, 46.92	31	9
Tabae	Horn of Africa	11.82, 51.25	32	5
Opone	Horn of Africa	10.42, 51.27	30	7
Menuthias	East Africa	-6.13, 39.33	13	1
Nicon	East Africa	-1.22, 41.84	11	1
Pyralaae Islands	East Africa	-2.27, 40.9	11	1
Rhapta	East Africa	-7.85, 39.78	11	1
Sarapion	East Africa	2.03, 45.33	11	1
Cana	Arabia	14.03, 48.34	36	16
Dioscorida	Arabia	12.51, 53.92	11	10
Moscha	Arabia	17.04, 54.43	5	8
Muza	Arabia	13.32, 43.25	47	11
Ocelis	Arabia	12.77, 43.65	14	3
Sarapis	Arabia	20.47, 58.82	1	1
Apologus	Persia	30.89, 47.58	12	4
Ommana	Persia	24.34, 56.73	16	6
Oraea	Persia	25.21, 64.63	8	1
Ariaca	Scythia	23.06, 70.62	19	7
Barbaricum-Minnagara	Scythia	24.86, 67.01	22	1
Bacare	India	9.59, 76.49	34	6
Barygaza	India	21.71, 72.99	64	15
Camara	India	11.14, 79.86	13	5
Muziris	India	10.16, 76.21	34	7
Nelcynda	India	9.32, 76.54	34	6
Paethana	India	19.48, 75.38	1	1
Poduca	India	11.9, 79.82	13	5
Sopatma	India	12.53, 80.16	13	5
Tagara	India	18.32, 76.13	4	1
Tyndis	India	10.77, 75.9	34	6
Besatae	East Asia	27.33, 88.62	1	5

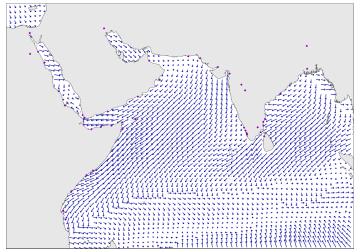
Note: This table only includes cities that have both goods and partners listed in the text of [?]. Coordinates are in (Lat, Lon) (srmat; Goods includes the number of unique products the city trades (both imports and exports); Partners indicates the number of other cities a given oily trades with



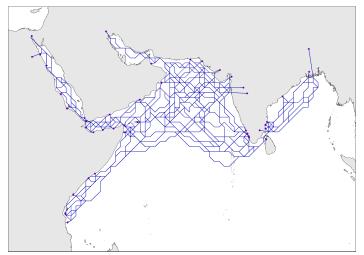
### **Summer Monsoon Winds**



### Winter Monsoon Winds



### Winter Monsoon Routes



Following Eaton and Kortum (2002):

 $z_j(g)$  is city j's efficiency of producing good g

City-specific probability distribution  $F_j(z) = Pr[Z_j \le z]$  Fréchet Type II distribution:

$$F_j(z) = e^{-T_j z^{-\theta}}$$

 $T_j > 0$  is a city specific parameter  $\theta > 1$  is a parameter for the variation in the distribution



Cost of delivering a unit of good g produced in city j to city i is

$$p_{ij}(g) = \left(\frac{c_j}{z_j(g)}\right) d_{ij}$$

 $c_j$  is the cost of all inputs, including labour  $d_{ij}$  is an iceberg transport cost

Consumers choose goods from destinations that minimise price

The price of good g in i will be the lowest across all N sources:

$$p_i(g) = \min\{p_{ik}(g); k = 1, ..., N\}$$



The price distribution for what city *n* actually buys is:

$$G_i(p) = Pr[P_i \le p] = 1 - \prod_{j=1}^{N} [1 - G_{ij}(p)]$$

inserting the price distribution function collapses the function into something resembling  $G_{ii}(p)$ :

$$G_i(p) = 1 - e^{-\Phi_i p^{\theta}}$$

where

$$\Phi_i = \sum_{i=1}^N T_j (c_j d_{ij})^{-\theta}$$



The probability that city *j* provides a good at the lowest price in destination *i* is

$$\pi_i = \frac{T_j(c_j d_{ij})^{-\theta}}{\Phi_i}$$

which is equivalent to the contribution of city *j* to city *i*'s price parameter

Average expenditure of city i on each good does not vary by source, so the proportion of goods city i buys from city j is the proportion of its expenditure on goods from city j:

$$\pi_{ij} = \frac{X_{ij}}{X_i} = \frac{T_j(c_j d_{ij})^{-\theta}}{\Phi_i} = \frac{T_j(c_j d_{ij})^{-\theta}}{\sum_{j=1}^{N} T_j(c_j d_{ij})^{-\theta}}$$



This expression can be rearranged into a equation resembling a basic gravity function:

$$X_{ij} = \frac{T_{j}(c_{j}d_{ij})^{-\theta}X_{i}}{\sum_{j=1}^{N}T_{j}(c_{j}d_{ij})^{-\theta}}$$

using market clearing conditions, this can be turned into a standard gravity equation in the normal way:

$$X_{ij} = \frac{X_i X_j}{X_w} \left( \frac{d_{ij}}{\Phi_j \Phi_i} \right)^{-\theta}$$

where  $X_w = \sum_k X_k$  is total output and  $\Phi_j$  and  $\Phi_i$  serve as multi-lateral resistance terms.



### Sector Data Table

Manufactures: Product	Product Category	Product	Product Category
Palm Oil	Plant Products	Robes	Textiles
Sesame Oil	Plant Products	Skin Coats	Textiles
Coloured Lac	Dye	Thin Clothing	Textiles
Purple	Dye	Tunics	Textiles
Wine	Wine	Indian Cloth	Textiles
Awls	Finished Products	Cloth	Textiles
Daggers	Finished Products	Cotton Cloth	Textiles
Hatchets	Finished Products	Mallow Cloth	Textiles
Images	Finished Products	Monache Cloth	Textiles
Lances	Finished Products	Muslins	Textiles
Sewn Boats	Finished Products	Purple Cloth	Textiles
Native Produce	Finished Products	Raw Silk	Textiles
Arabian Clothing	Textiles	Sagmatogene Cloth	Textiles
Blankets	Textiles	Silk Cloth	Textiles
Cloaks	Textiles	Silk Yarn	Textiles
Coloured Sashes	Textiles	Flint Glass	Gems & Glass
Girdles	Textiles	Glass	Gems & Glass
Local Clothing	Textiles	Murrhine Glass	Gems & Glass
Spices & Aromatics	s:		
Product	Product Category	Product	Product Category
Indian Copal	Plant Products	Spikenard	Incense & Spices
Aloes	Plant Products	Storax	Incense & Spices
Macir	Plant Products	Cinnamon	Incense & Spices
Duaca	Incense & Spices	Malabathrum	Incense & Spices
Fragrant Ointments	Incense & Spices	Pepper	Incense & Spices
Frankincense	Incense & Spices	Spices	Incense & Spices
Myrrh	Incense & Spices		
Bullion:			
Product	Product Category		
Coin/Gold	Bullion		

Note: This table groups individual products from Table ?? into the sectoral categories that are included in the development analysis.